



**EPSRC**

Engineering and Physical Sciences  
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NOTTINGHAM  
TRENT UNIVERSITY 

# Acoustic Wave Sensors: Modes, Responses and Hydrophobicity

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MicroNanoacoustics Workshop, Prato, Italy

[www.naturesraincoats.org](http://www.naturesraincoats.org)

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# Overview

## 1. Basics of Acoustic Wave Sensors

- Acoustic waves: Modes and devices
- Sensing principles: Solids and liquids

## 2. Layer-Guided Acoustic Waves

- Love waves & acoustic plate modes
- Layer-guided devices: Operating points and sensitivity

## 3. Sensor Research Examples

- Steroids: Molecularly imprinted polymers
- Cancer vaccines: Peptide binding

## 4. Current Acoustics Research

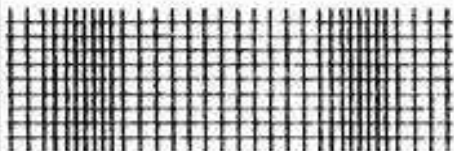
- VetAI: Sperm motility
- Green solvents: Ionic liquids and microfluidics
- Wetting: Hydrophobicity and slip on topographically structured surfaces

# Basics of Acoustic Waves

# Acoustic Waves

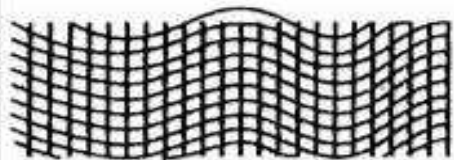
## Acoustic Waves

bulk longitudinal wave



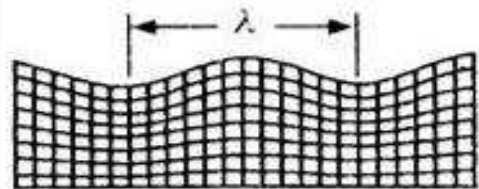
$$v_p = 4000\text{--}12000 \text{ m s}^{-1}$$

bulk transverse wave



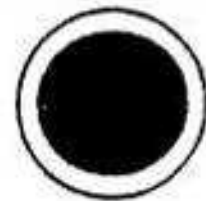
$$v_p = 2000\text{--}6000 \text{ m s}^{-1}$$

surface (Rayleigh) wave



$$v_p = 2000\text{--}6000 \text{ m s}^{-1}$$

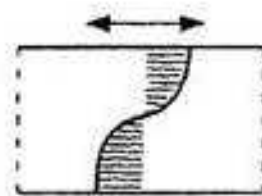
## QCM versus SAW



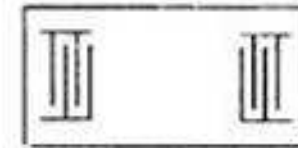
top



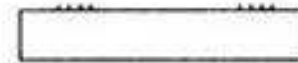
side



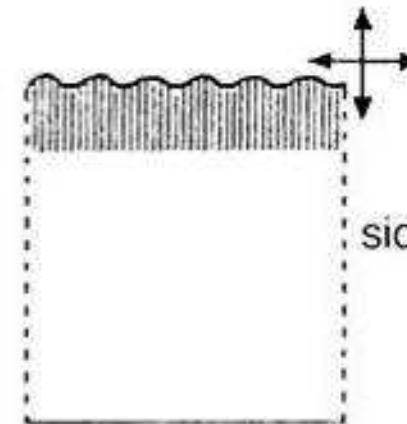
side



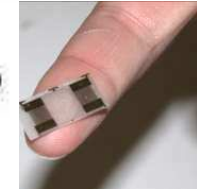
top



side



side

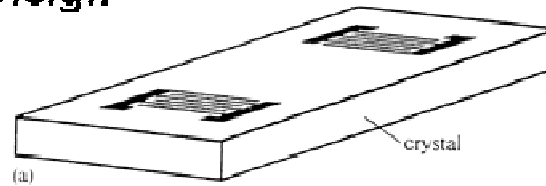


*QCM – frequency determined by thickness*  
*SAW – frequency determined by fingers*

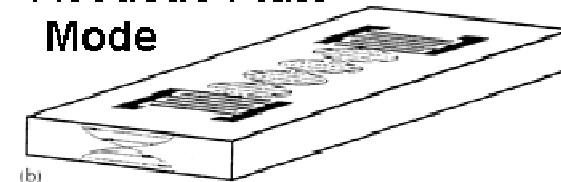
# Acoustic Wave Modes

## Delay Lines

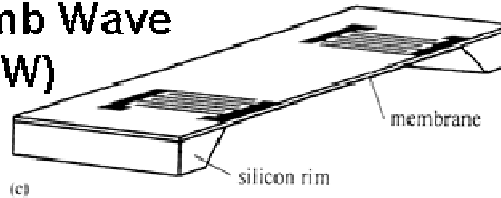
**Rayleigh**



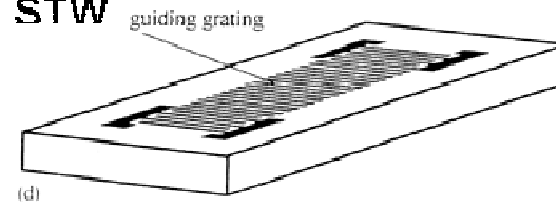
**Acoustic Plate Mode**



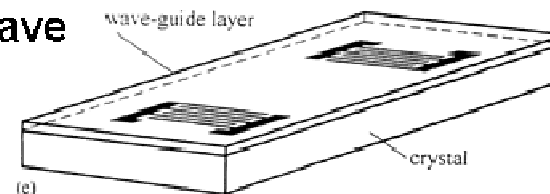
**Lamb Wave (FPW)**



**STW**



**Love Wave**



<u>Mode</u>	<u>Rel. Sens.</u>	<u>Complexity</u>	<u>Robustness</u>	<u>Gas/Liquid</u>
QCM	Low	Low/Xtal	Med	g+l
SAW	High	Med/metal on Xtal	High	g
Love	High	Med/film+metal+Xtal	High	g+l
STW	High	Med/metal on Xtal	High	g+l
Lamb	High	High/membrane	Low	g+l
APM	Med	Med/metal on Xtal	Med	g+l

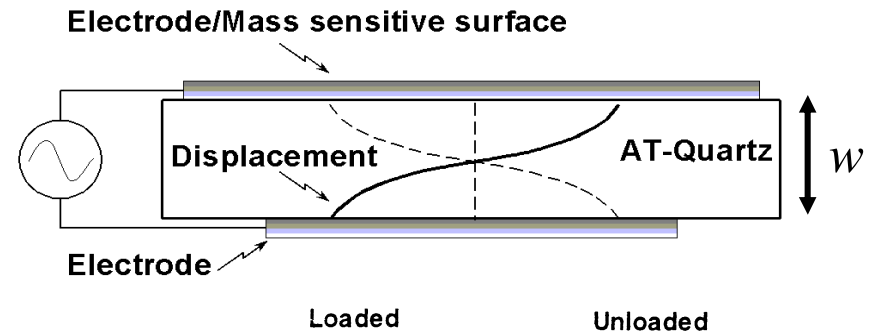
# QCM/QCR Sensing Principles

## Thickness Shear Mode Vibration

QCM has a sharp resonance

Frequency given by quartz thickness,  $w$

$$v_s = f\lambda \Rightarrow f = 2v_s/w$$



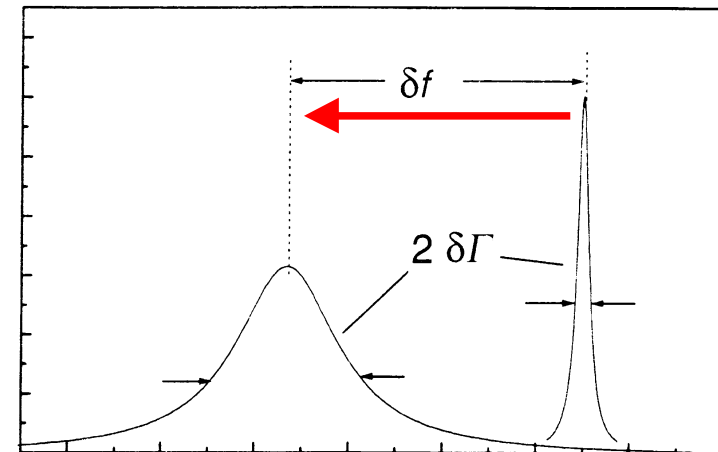
## Mass Loading or Immersion

QCR resonant frequency reduces due to mass

Resonance broadens due to polymer/liquid

Sauerbrey equation  $\Rightarrow \Delta f \propto -f^2 \Delta m/A$

Kanazawa & Gordon  $\Rightarrow \Delta f \propto -\sqrt{(\eta\rho)} f^{3/2}$



- 1. Increasing mass or viscosity-density product decreases resonant frequency*
- 2. Increasing viscosity-density product (or polymer) broadens resonance*

# Liquids and Penetration Depth

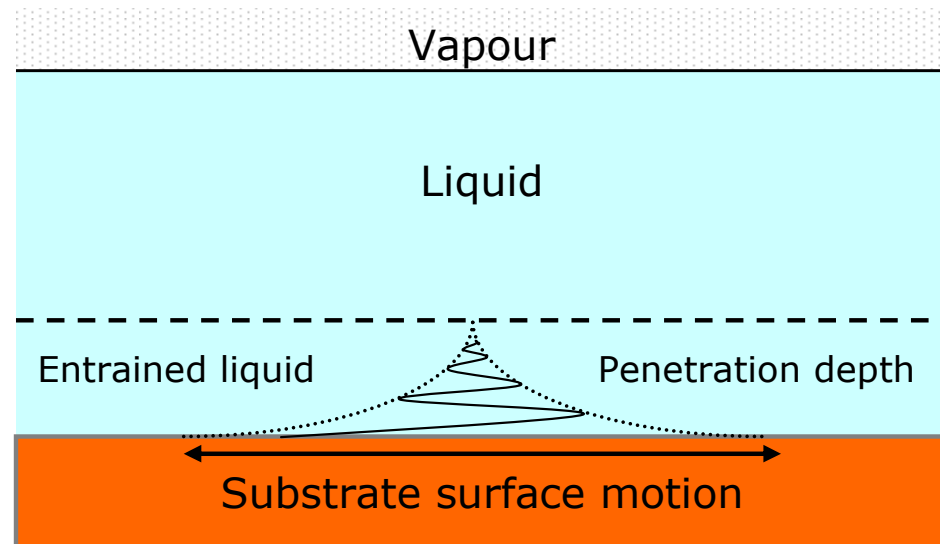
## Shear Mode Vibration

Entrains liquid

Liquid oscillation decays

Penetration depth

$$\delta = (\eta / \pi f \rho)^{1/2}$$



## Liquid Sensing

Sense liquid mass (via viscosity-density product) within penetration depth

QCM

SAW

For water:

5 MHz

$\delta \sim 250$  nm

500 MHz

$\delta \sim 25$  nm

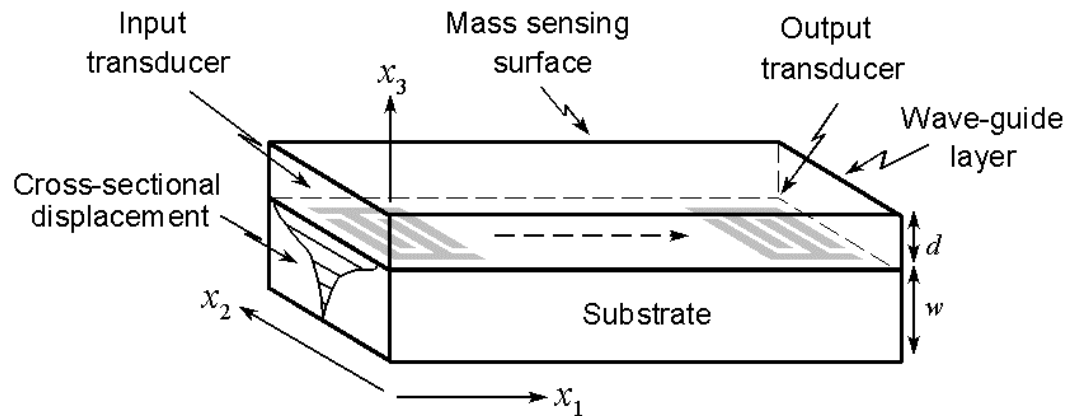
- 1. Penetration depth gives sensing zone which decreases with frequency*
- 2. Penetration depth/sensing zone increases with viscosity*

# Layer-Guided Acoustic Waves



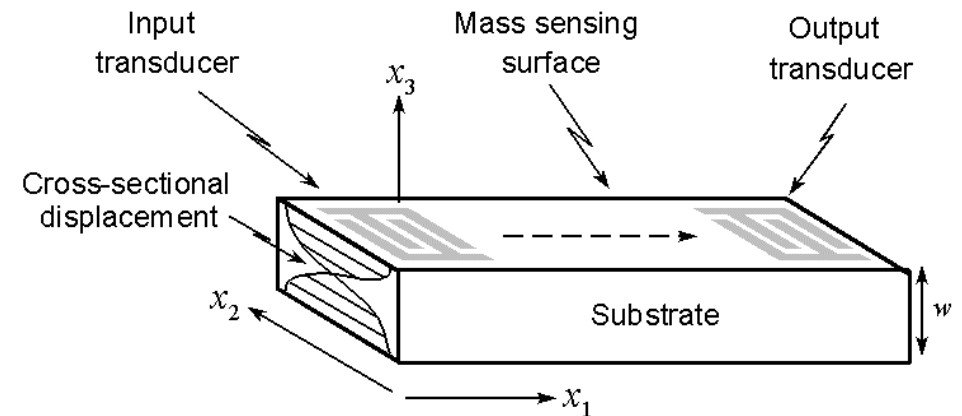
# Love Waves versus SH-APMs

## Love Wave



Layer guided SH-SAW with  $v_l < v_s$   
Surface localised wave  
Increased sensitivity

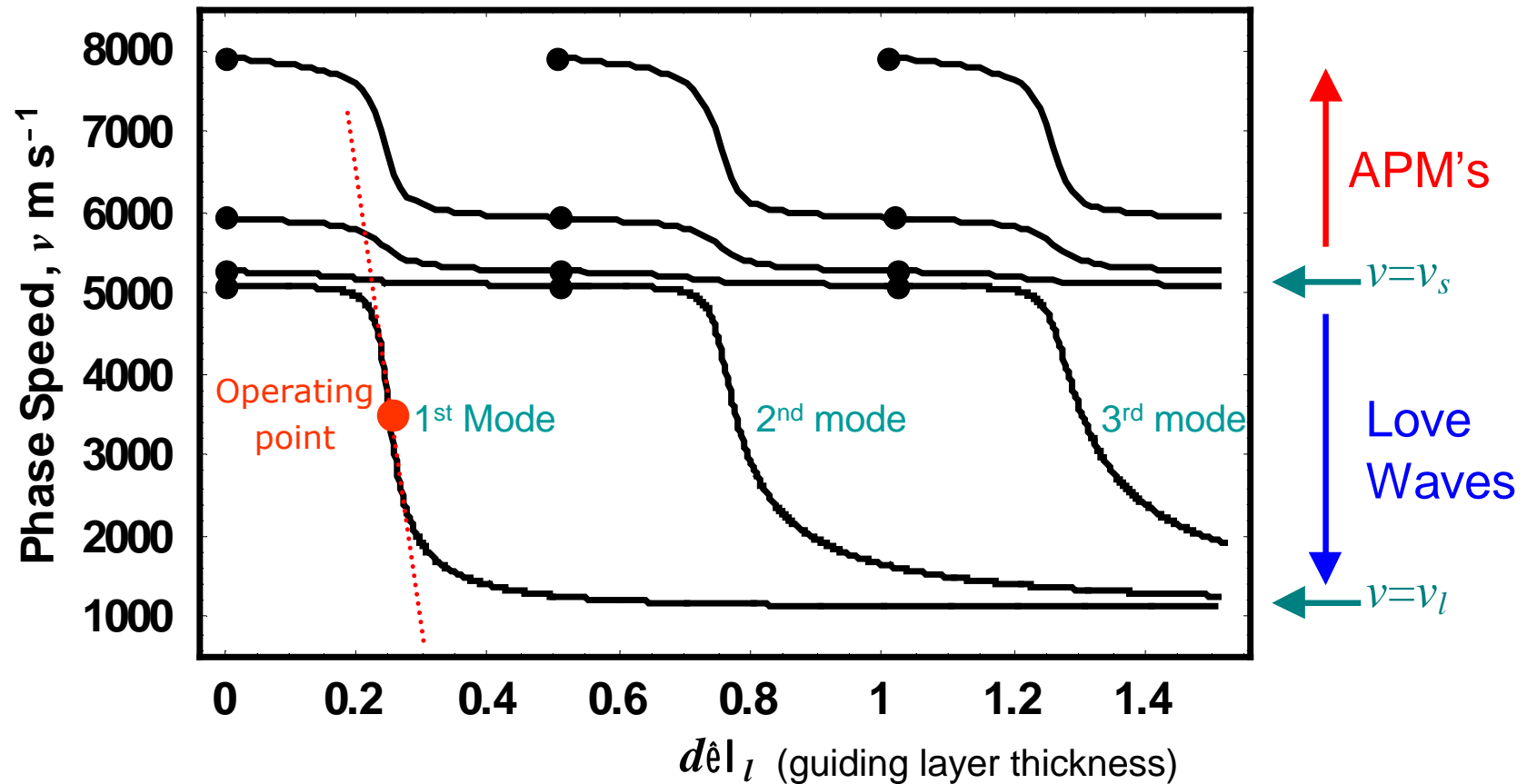
## SH-APM



“QCM with propagation”  
Substrate resonance  
Sensing via both faces

*Increased sensitivity versus isolation between sensing face and transduction*

# Generalized Love Waves – Operating Point



$\nu > \nu_s$ : Plate modes = Switch in order of resonance induced by layer

$\nu < \nu_s$ : Love wave = Shear mode in substrate-to-shear mode in layer transition

*Increased mass/liquid sensitivity related to slope of dispersion curve*

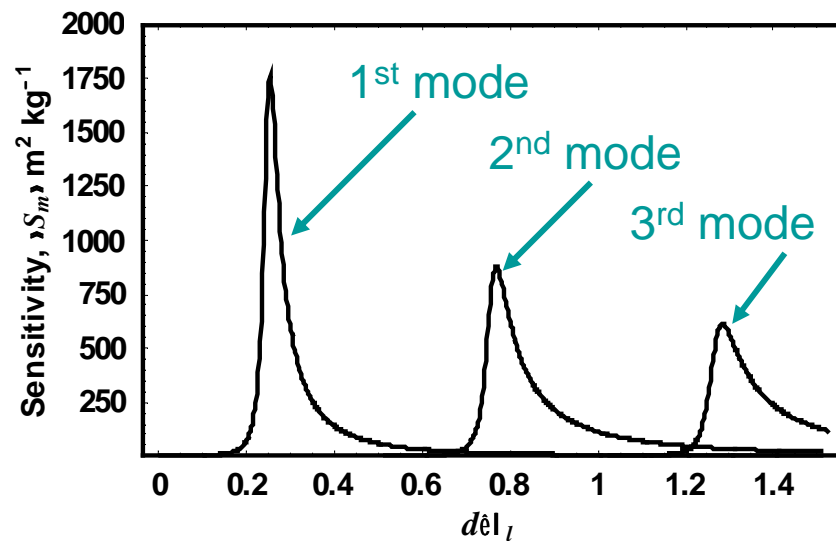
# Phase Speed Mass Sensitivity

$$S_m = \lim_{\Delta m \rightarrow 0} \frac{1}{\Delta m} \left( \frac{\Delta v}{v_o} \right) \approx \frac{f_o}{\rho_l |v_l|} \left( \frac{d \log_e v}{dz} \right)_{z_0}$$

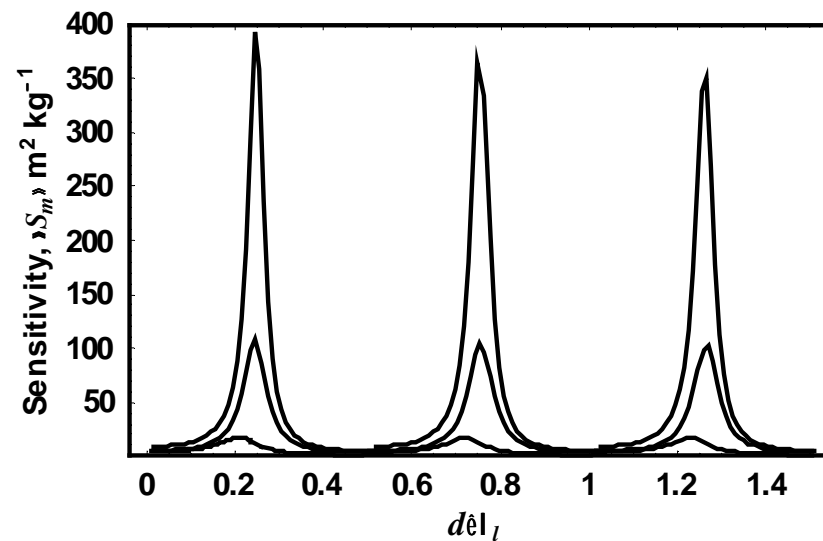
$\Delta m$  is mass per unit area being sensed,  $z = df/v_l$  is the normalized thickness

"Rigid" mass  $\Rightarrow$  Mass sensitivity is slope of dispersion curve

## Love Waves



## Layer-Guided SH-APMs



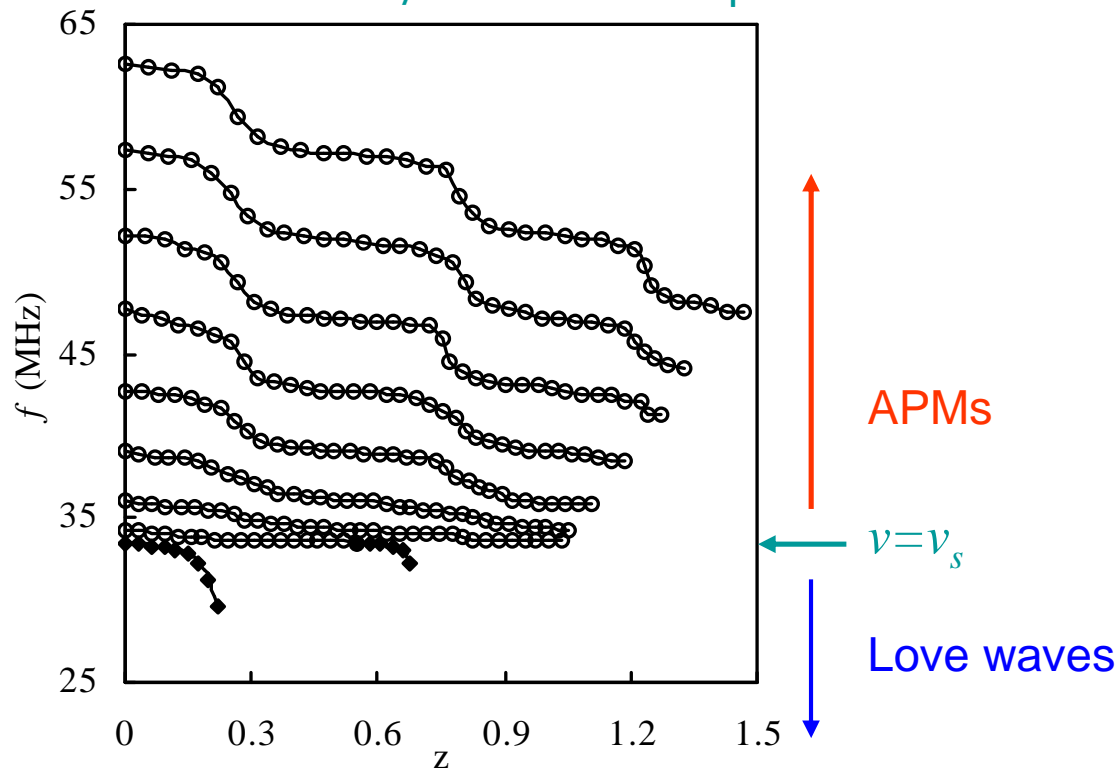
# Experimental Data for Layer-Guided SH-APMs

25 MHz surface skimming bulk wave (SSBW)

Propagation orthogonal to x-axis of thinned (200  $\mu\text{m}$ ) ST-Q substrate

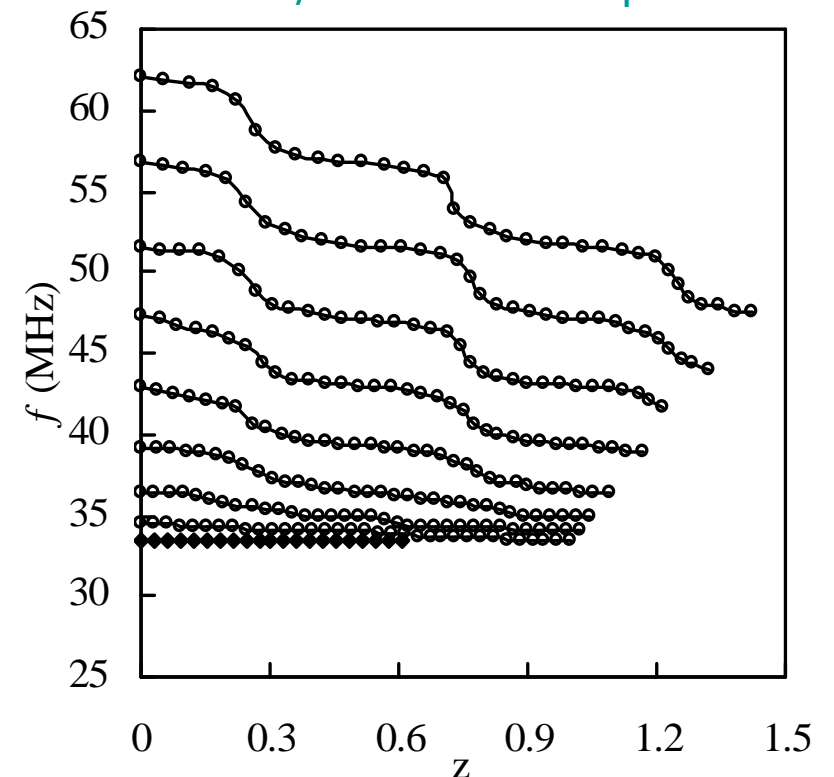
## IDT Face Coated

Love wave and SH-APM  
are both sensitive  
x-axis is  $d/\lambda$  with  $\lambda$ =IDT period



## Opposing Face to IDTs Coated

SH-APM changes  
Love wave insensitive  
x-axis is  $d/\lambda$  with  $\lambda$ =IDT period



# Generalized Sauerbrey/Kanazawa & Gordon

## Polymer Waveguide on Polymer Substrate

Complex velocity shift

$$\frac{\Delta v}{v_o} \approx \left( \frac{1 - v_f^2/v_o^2}{1 - v_l^2/v_o^2} \right) \left( \frac{d \log_e v}{dz} \right)_{z=z_o} \left( \frac{\tan(T_f^o h)}{T_f^o h} \right) \frac{\omega \rho_f h}{2\pi v_l^\infty \rho_l}$$

Complex slope factor  
from polymer waveguide

$\omega \Delta m/A$

$(\rho \eta \omega)^{1/2}$

tanx/x factor gives mass/liquid loading limits

$$\left( \frac{\tan(T_f^o h)}{T_f^o h} \right) \rightarrow \begin{cases} 1 & h \rightarrow 0 \\ \frac{-\sqrt{-2j}}{2h(1 - v_f^2/v_o^2)} \sqrt{\frac{2\eta_f}{\omega \rho_f}} & h \rightarrow \infty \text{ and } \omega \tau \rightarrow 0 \end{cases}$$

Sauerbrey/  
solid limit

Kanazawa &  
Gordon/liquid limit

# Sensor Research Examples

*(Selected) Past Work*

# Example 1: Steroids and MIPs

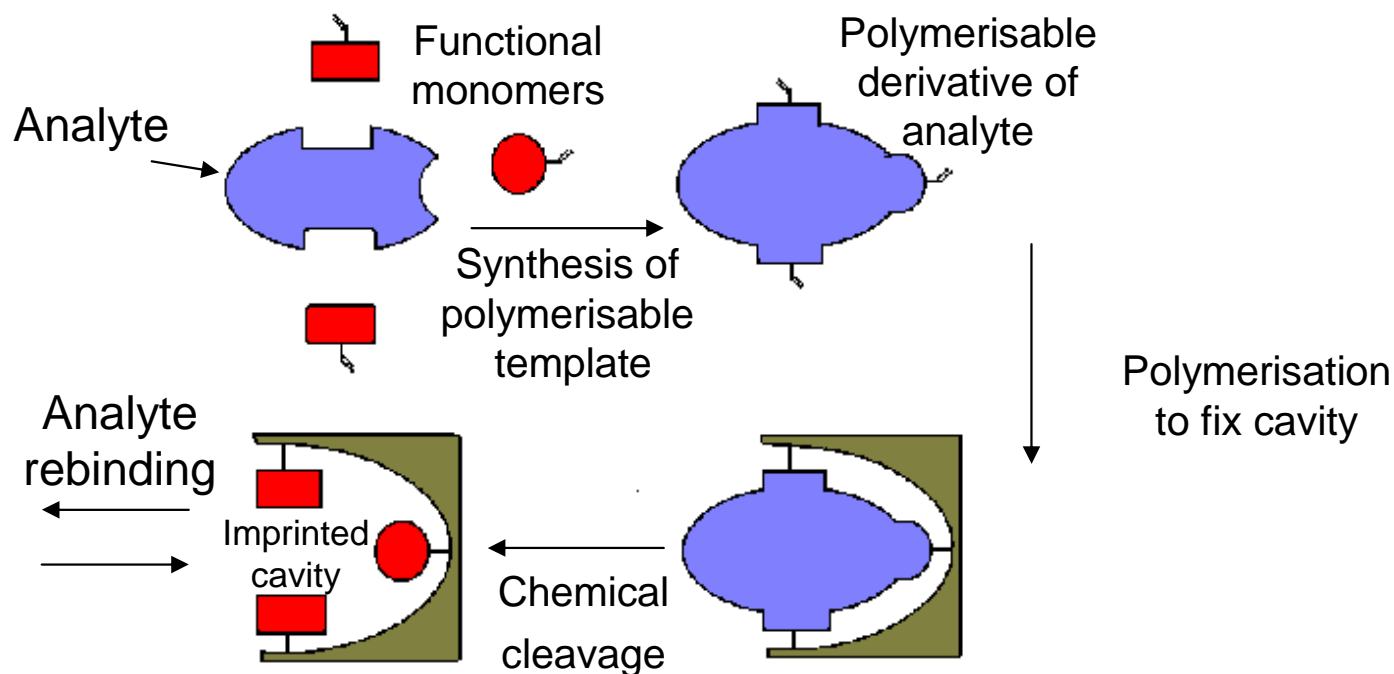
## Target Applications (*Liquid Phase*)

Recognition/selectivity via molecularly imprinted polymers (MIPs)

Applications: monoterpenes, amino acids, *topical steroids*

Tailor made enantioseparation materials

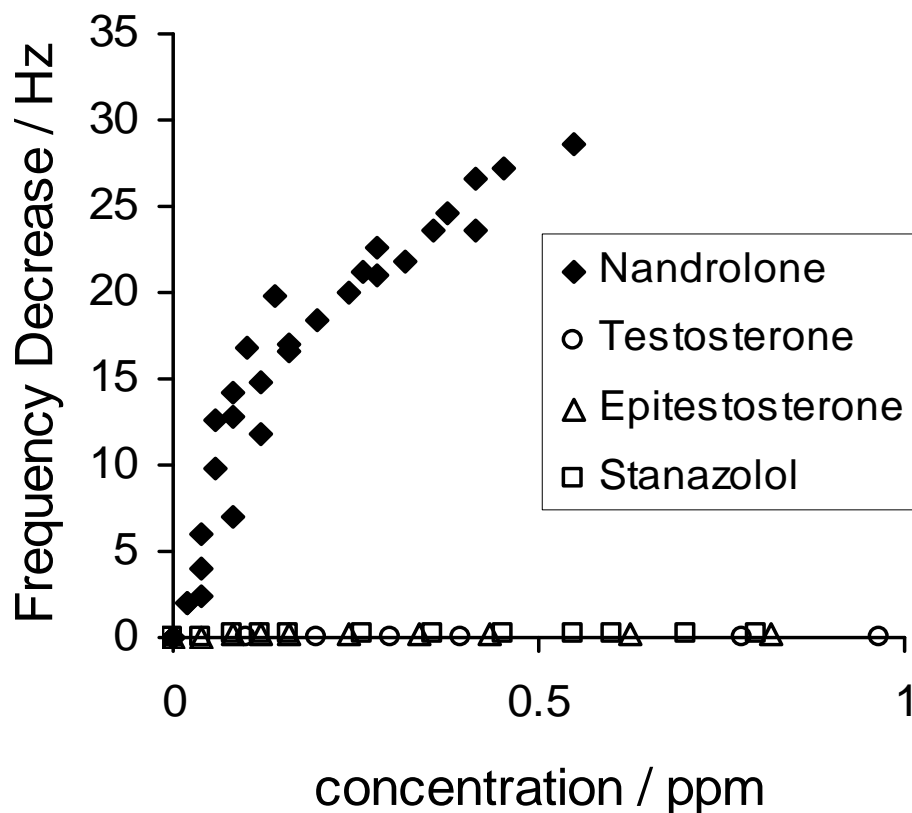
## MIP - Polymer Type Artificial Receptor



# Selectivity to Nandrolone

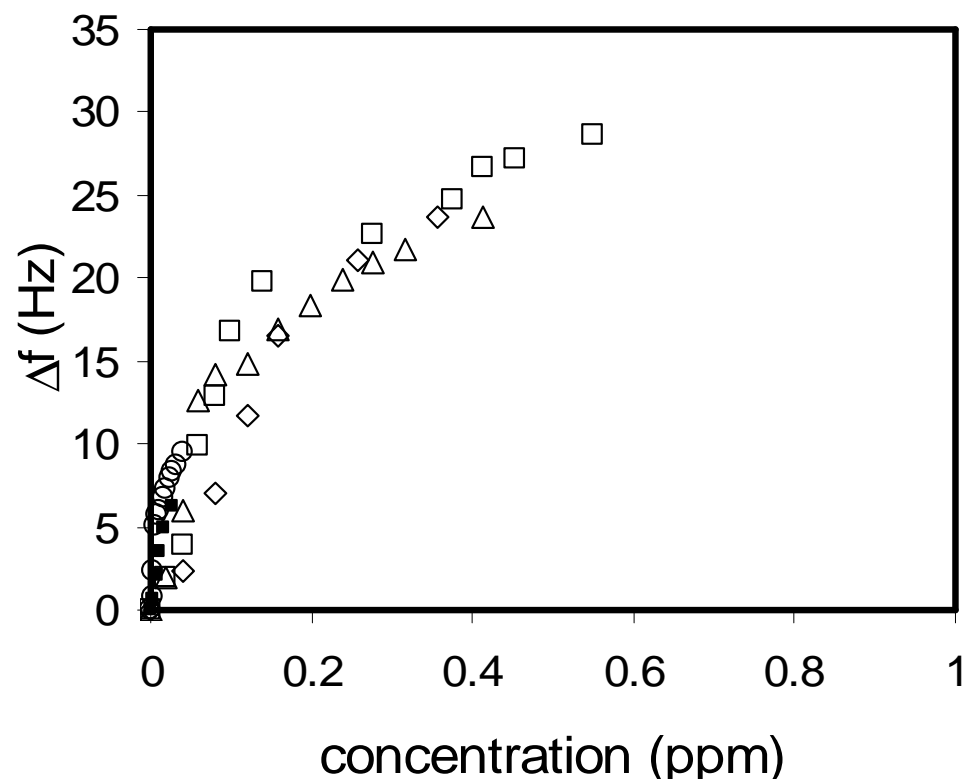
## QCM Coating

Spin coated/cast layer  
Covalent imprinting strategy



## Response to Replicates

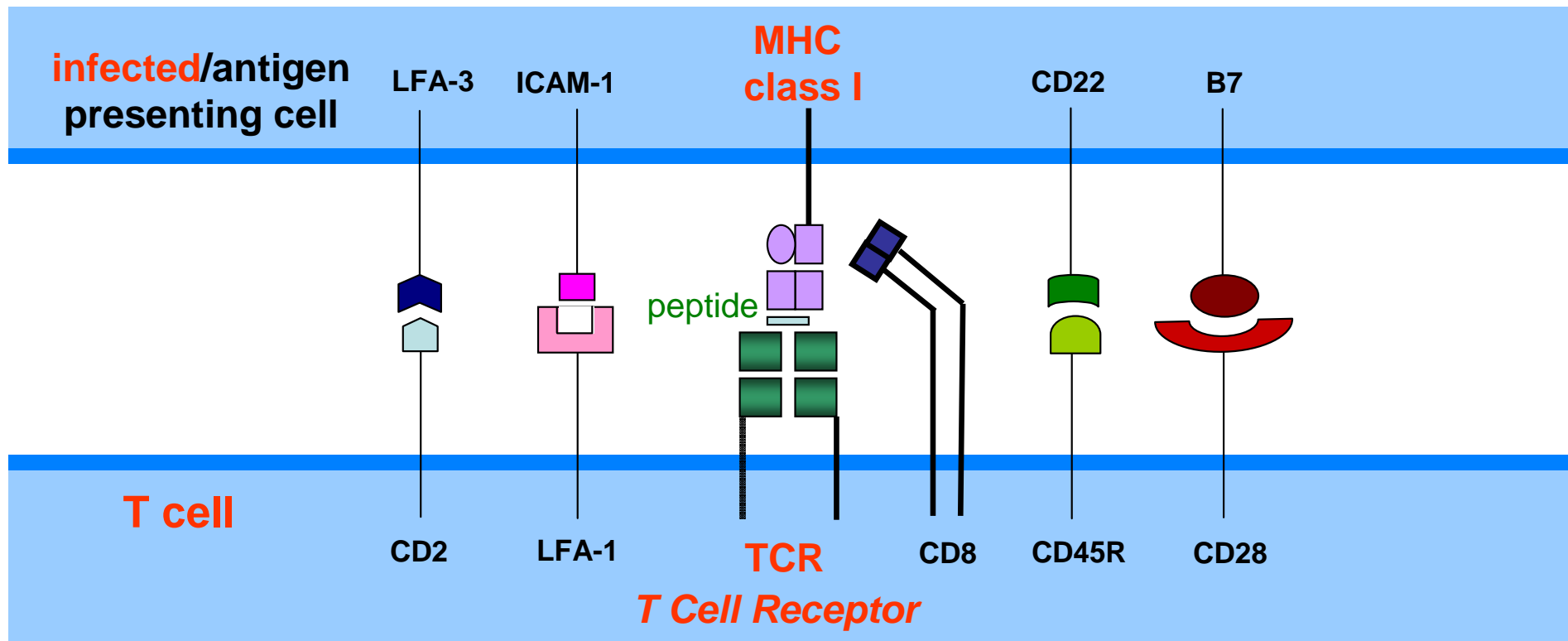
One-shot screening  
Test data for 5 crystals





# Example 2: Vaccines - Peptides and T-Cells

1. Infection/virus broken into peptide fragments and presented on cell surface
2. Cytotoxic T-cells attach to peptides and “read” peptide sequence
3. If foreign, cell is killed by release of a cytotoxic chemical
4. Major histocompatibility complex (MHC) antigens are responsible for the expression of peptides on the infected cell
5. Vaccine introduces peptide to the T-cell – Aim is to find suitable peptides



# Peptides and T-Cells

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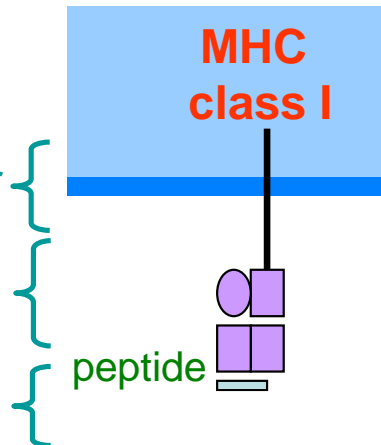
## Sensor Strategy

*Make this the acoustic wave sensor*

*Recognition layer is MHC protein*

*Detect peptide specific binding*

*Screen for suitable peptides (from the 1000's that exist) with specificity and strong affinity for the MHC*



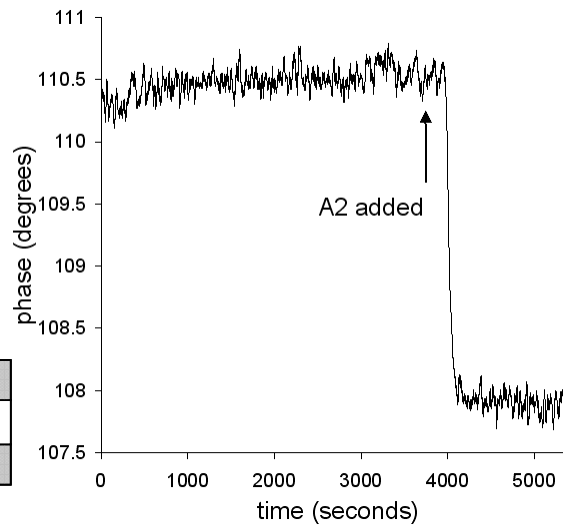
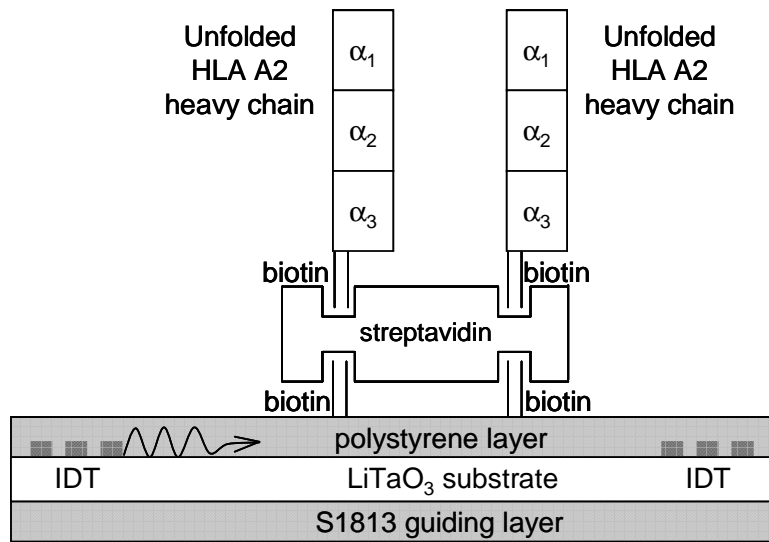
## Current State-of-Art

*Cellular peptide-MHC assays*

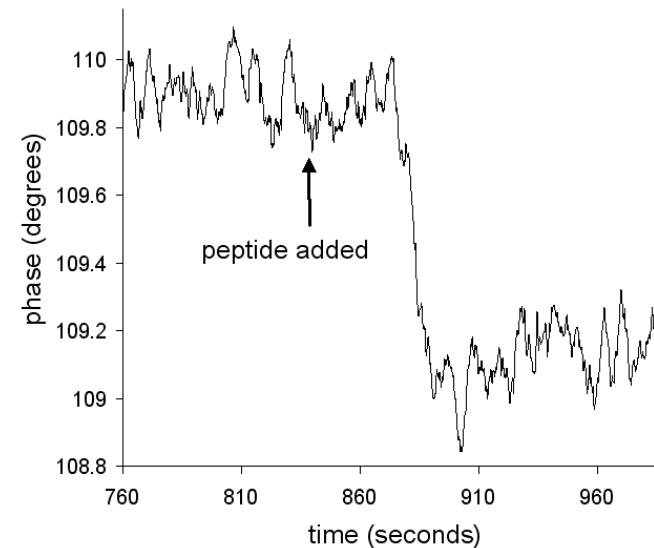
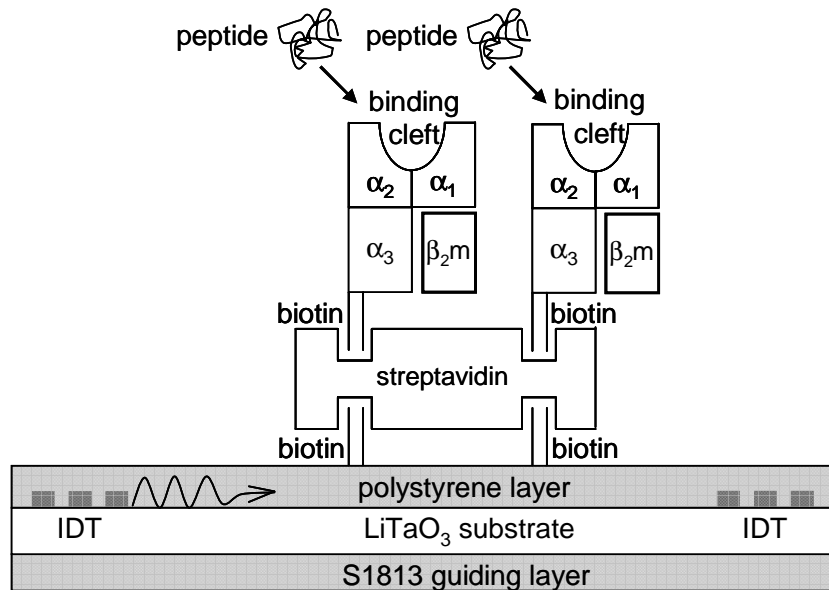
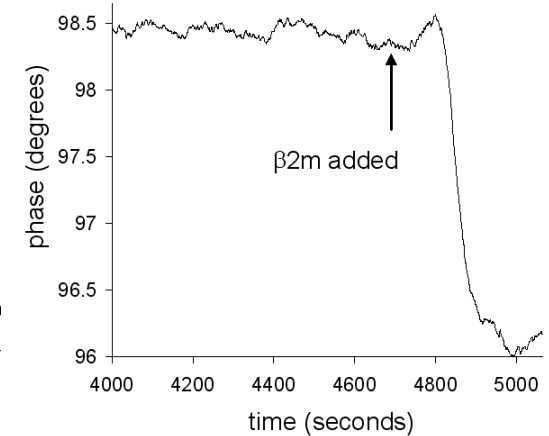
*→ yes/no and not real-time*

*Sensitive, real-time and non-cellular based assay would assist vaccine development*

# Flow Cell with Love Wave Screening Device



$\beta_{2m}$  protein binds to A2 and folds to create peptide specific binding cleft



# Acoustic Wave Research

## *Current Sensor Work*

# Project 1: Sperm Motility

## Veterinary Artificial Insemination (VetAI)

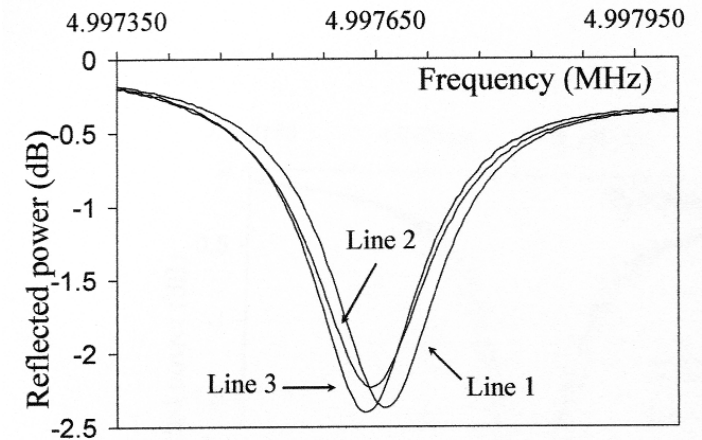
Sperm Quality Assessment & Detection Device (SQuADD)

Time of flight/swim

5 MHz QCM (or use other AWS device)

Frequency drop relative to reference

Crystal pre-coated with sperm 'sticky' material

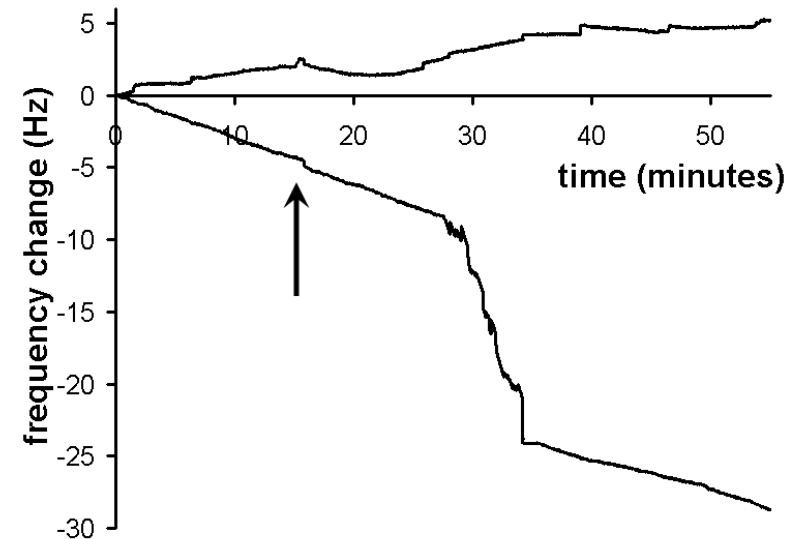


## Experimental Sequence

Stabilisation of signal in PBS

Addition of sperm (arrow)

Time of arrival data – swim speed



# Project 2: Ionic Liquids Chip

## Determining Physical Properties

- Room temperature ionic liquids (RTIL's)
- Green because non-volatile
- Millions of simple IL's, billions of binary ILs, ...
- Designer solvents
- Poorly characterised

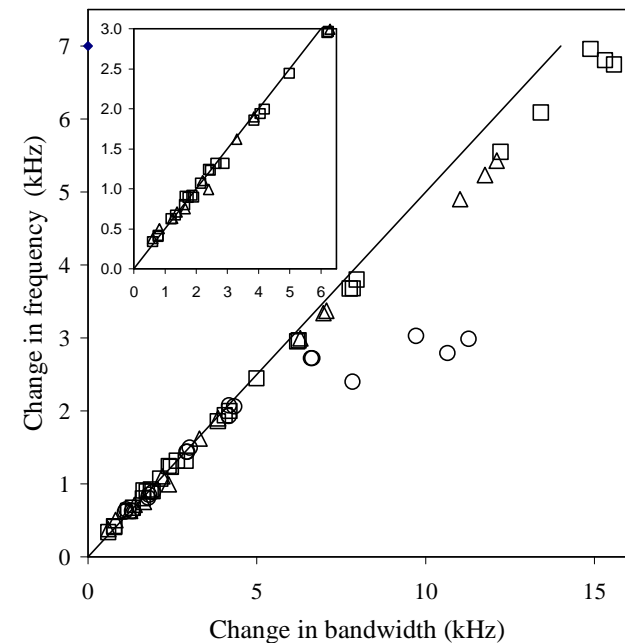
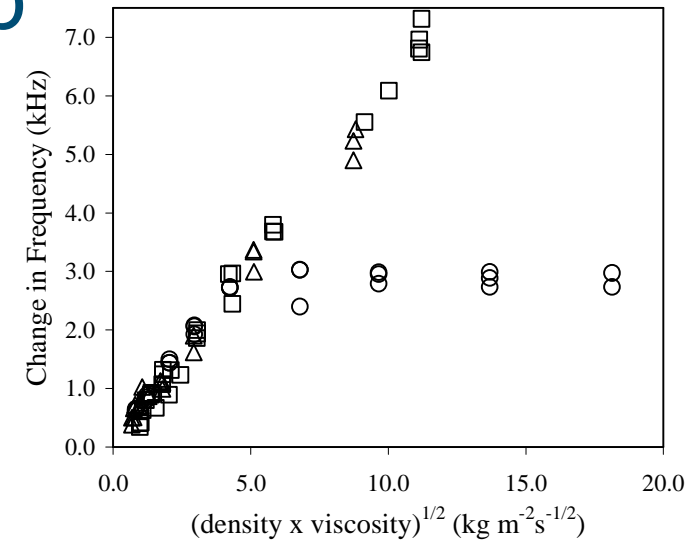
## QCM

- Can measure density-viscosity product, but can also determine whether Newtonian via coupled frequency shift-bandwidth increase

$$\Delta f = -\Delta B / 2$$

## Data

- Polydimethylsiloxane oil - known non-Newtonian at higher molecular weights (ooo)
- Two ionic liquids  $[C_4mim][OTf]$  ( $\square\square\square$ ) and  $[C_4mim][NTf_2]$  ( $\Delta\Delta\Delta$ )



# Chip Version – Dilutions of Ionic Liquids

## Experiment

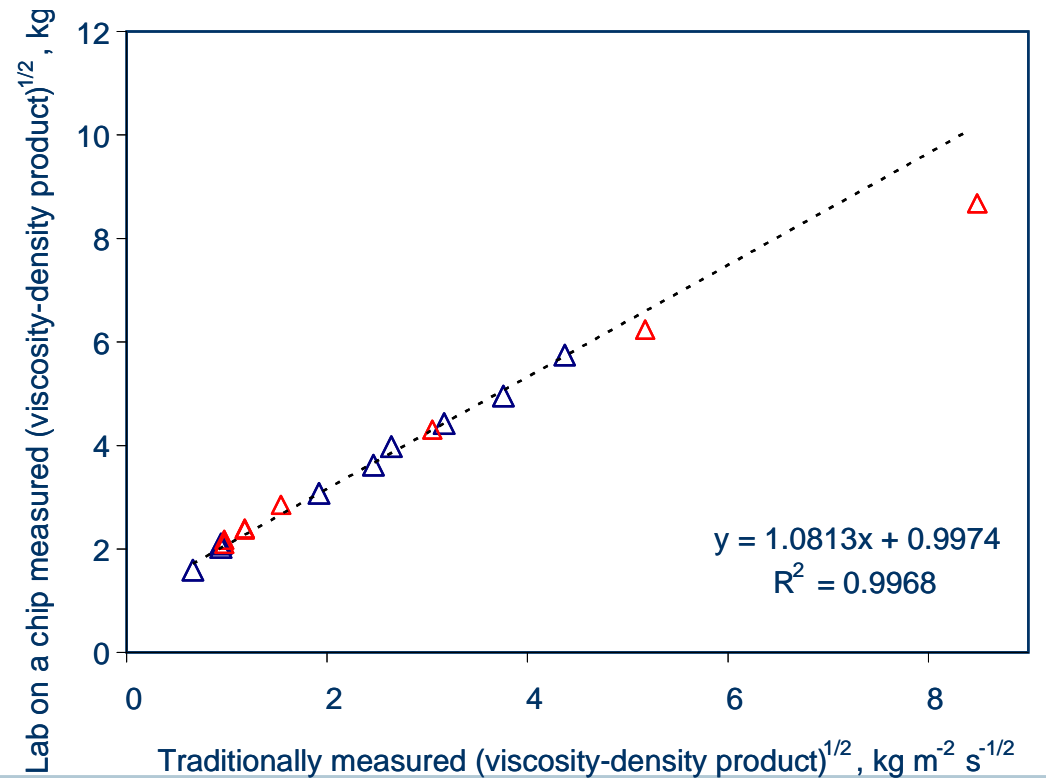
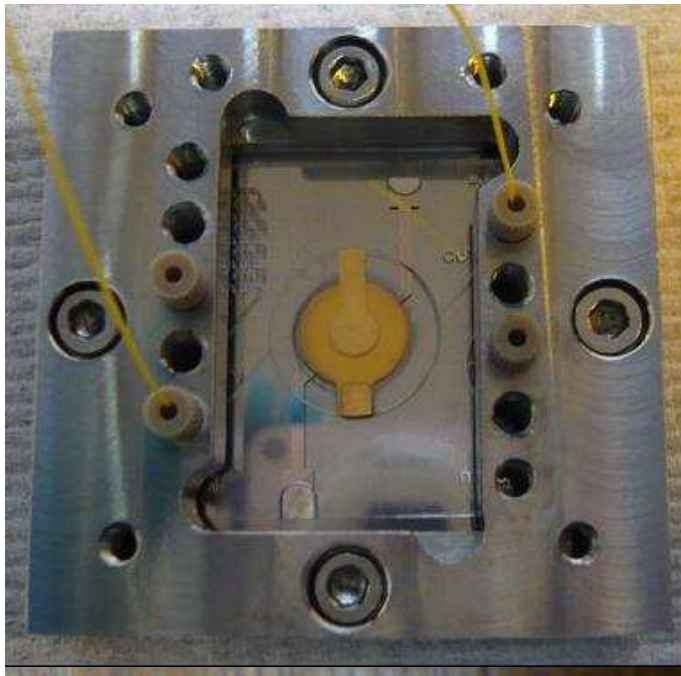
Sample: 30  $\mu\text{l}$  with 10  $\mu\text{l}$  in contact with QCM

QCM: 14 mm diameter, rough surface, 10 MHz operated at 3<sup>rd</sup> harmonic (30 MHz)

Flow-rate: 0.06  $\mu\text{l}/\text{s}$

Liquids: Glycerol/water and  $[\text{C}_4\text{mim}][\text{NTf}_2]/\text{methanol}$

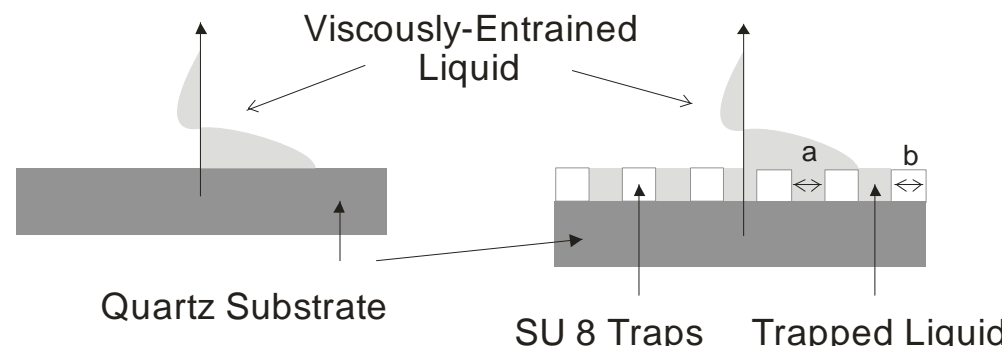
Also looked at smooth QCMs and pure ILs



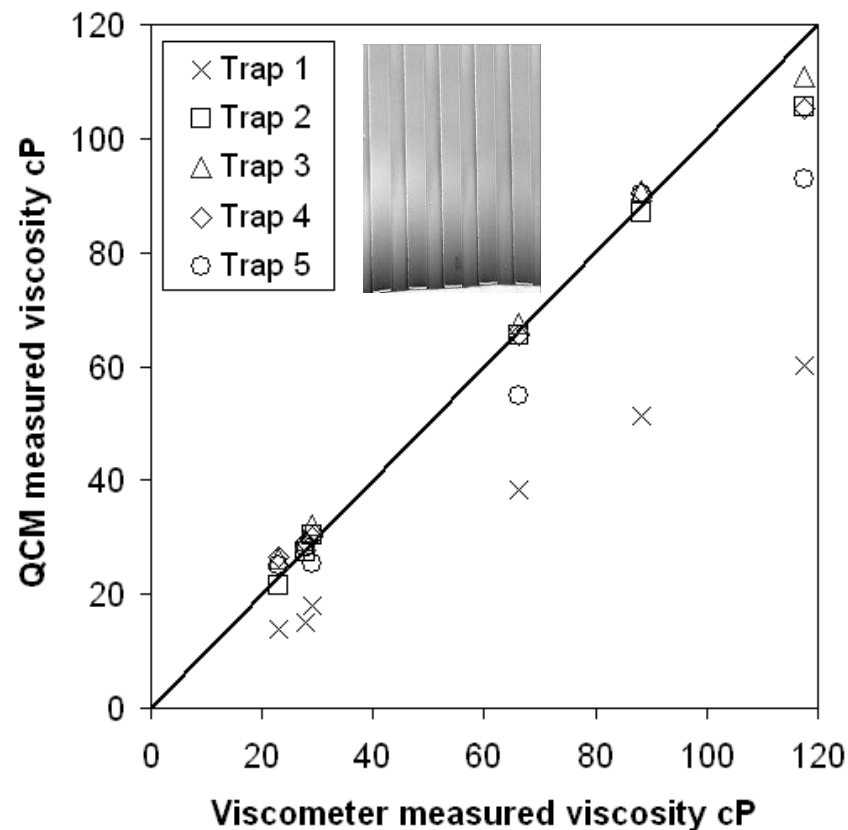
# Separating Viscosity from Density

## Original Concept (Martin *et al*)

- Dual QCM: Smooth and trap surfaces
- Frequency shifts allow separation of viscosity from density
- Our traps are fabricated using SU-8
- Various ionic liquids used
- Currently off-chip results



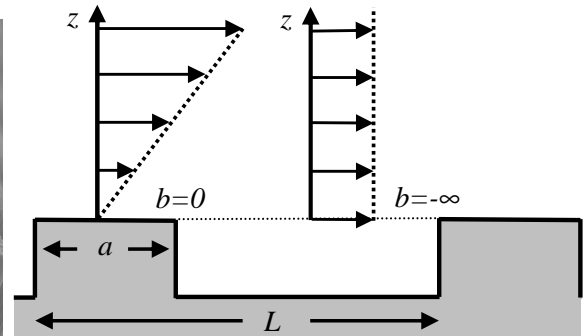
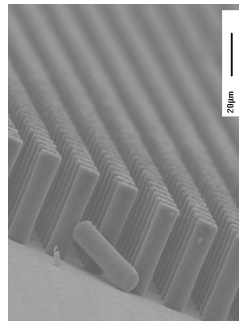
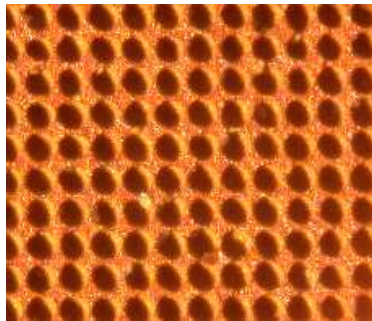
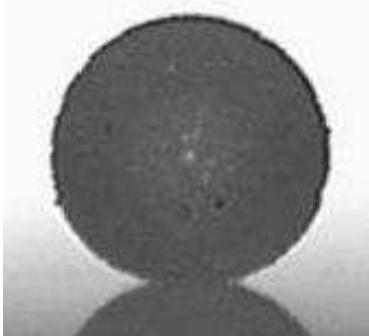
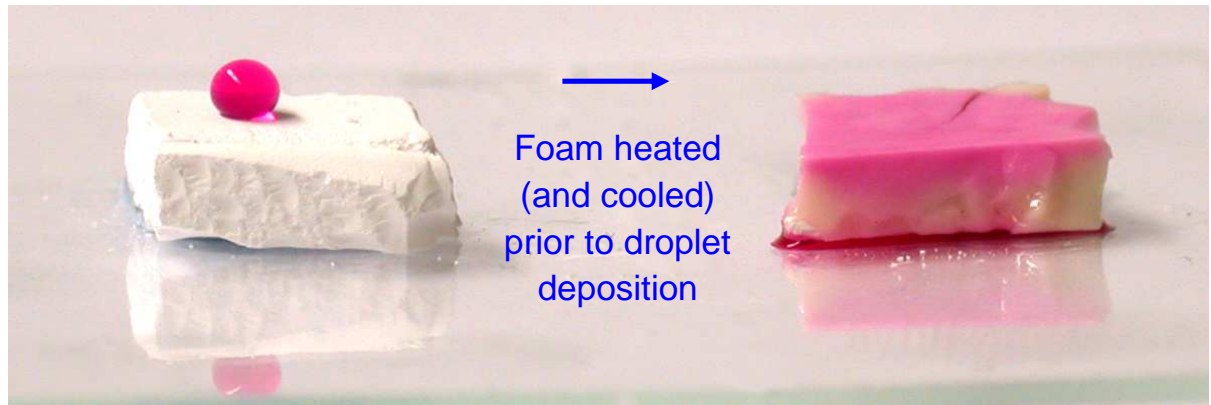
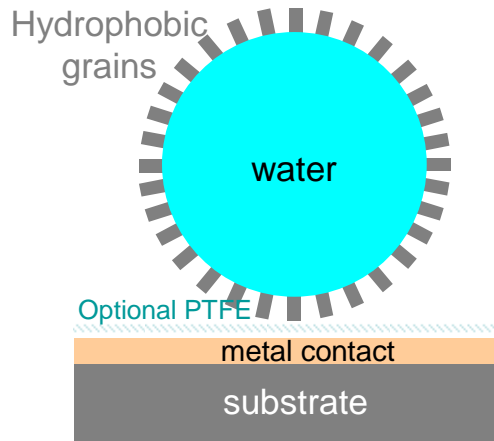
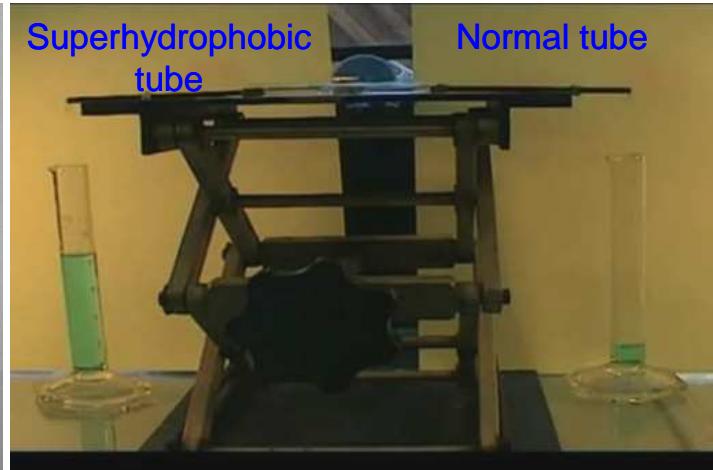
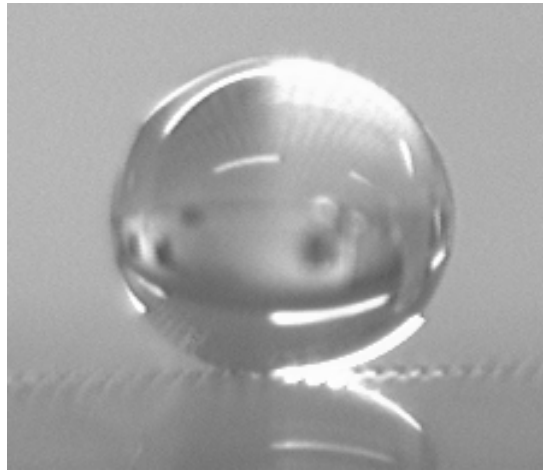
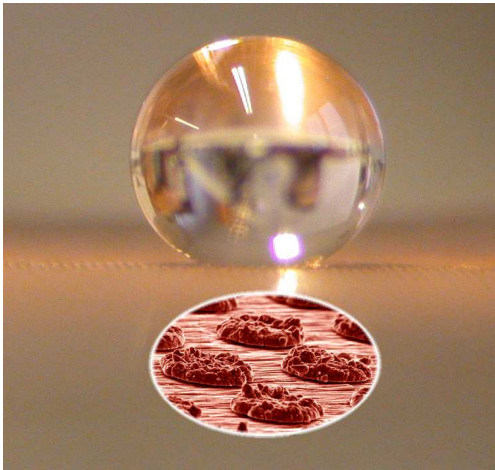
Trap	Width $\mu\text{m}$	Separation $\mu\text{m}$	Effective Height $\mu\text{m}$
1	10.7	30.4	0.838
2	24.1	34.5	2.118
3	43.3	52.5	1.818
4	70.5	84.0	1.419
5	108.0	97.0	1.277





# Acoustic Wave Research

## *Wetting and Acoustics Work*



# Old Work: SAWs and Stripes of Oil

## Determining Physical Properties

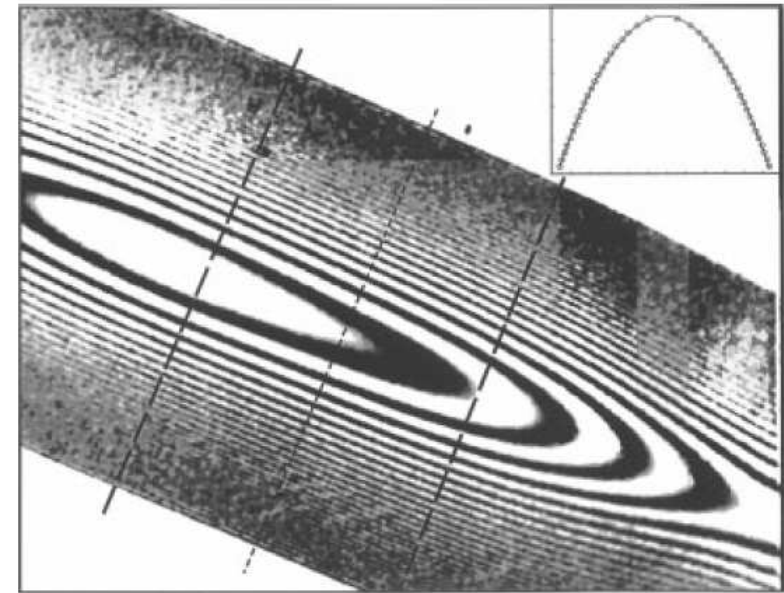
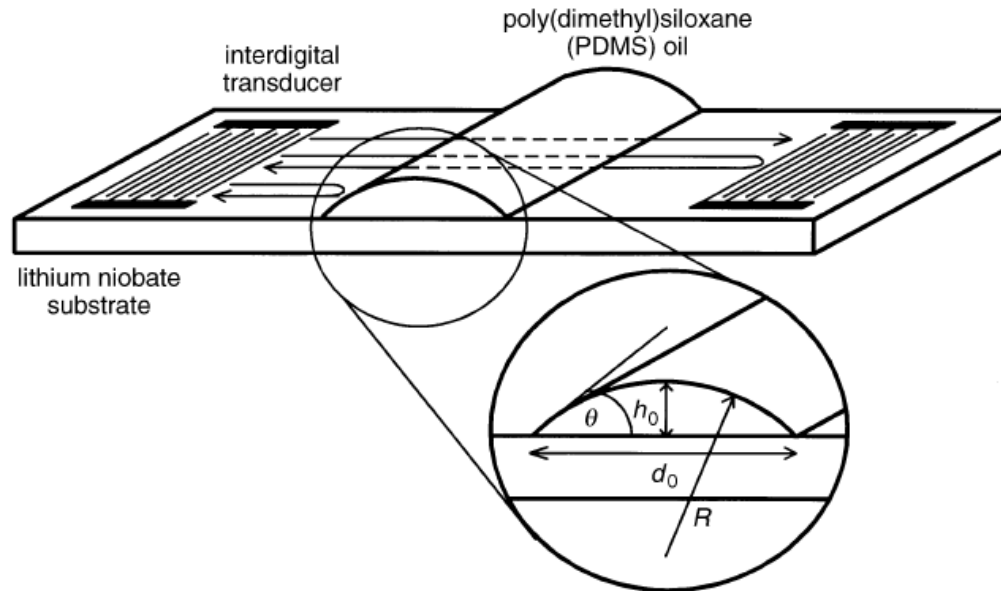
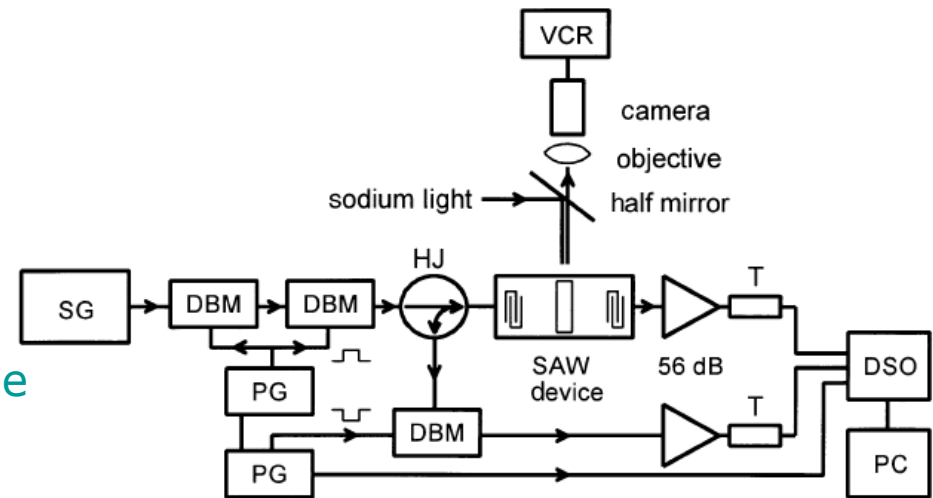
170 MHz Rayleigh SAW

Pulse mode

PDMS oils (10 000-100 000 cSt)

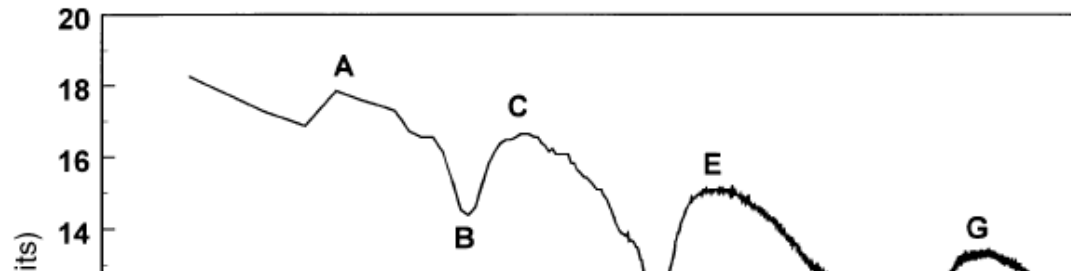
Attenuation and reflection of SAW

Simultaneous interferometry for shape

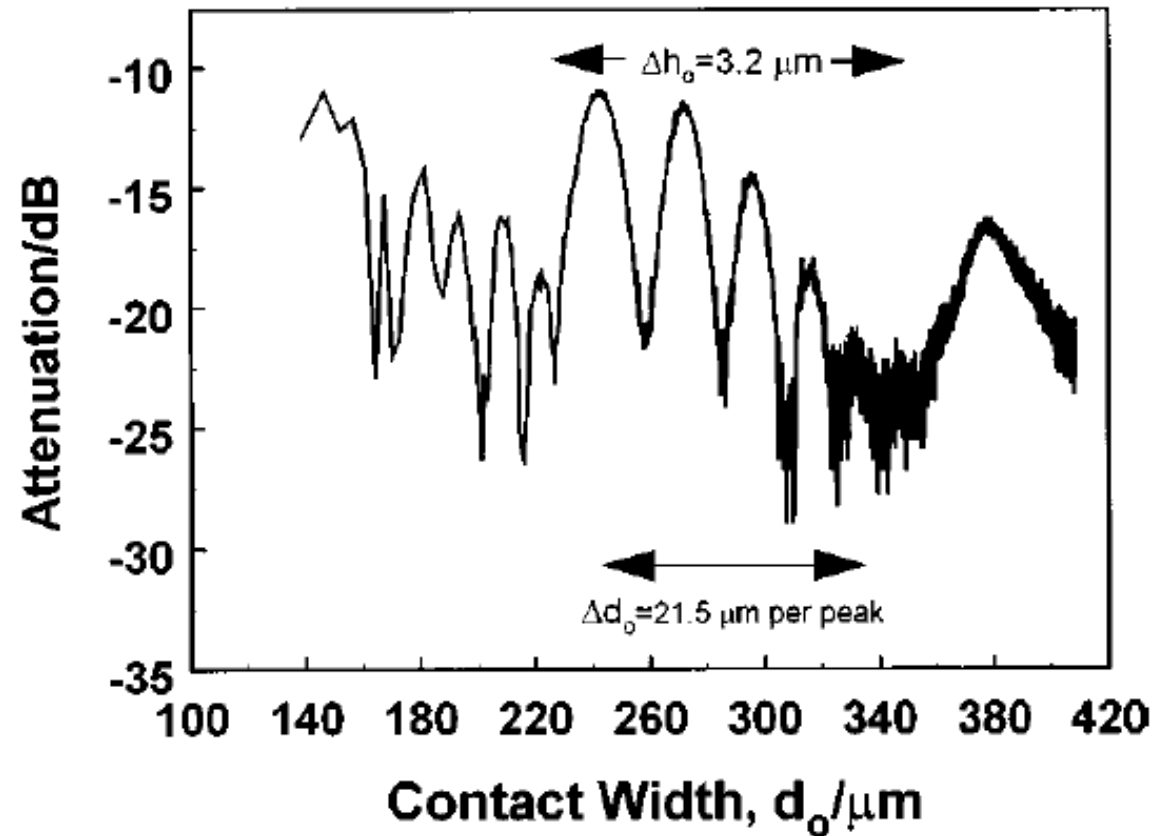


# Old Work: Attenuation and Reflections

Attenuation Data:



Reflection Data:

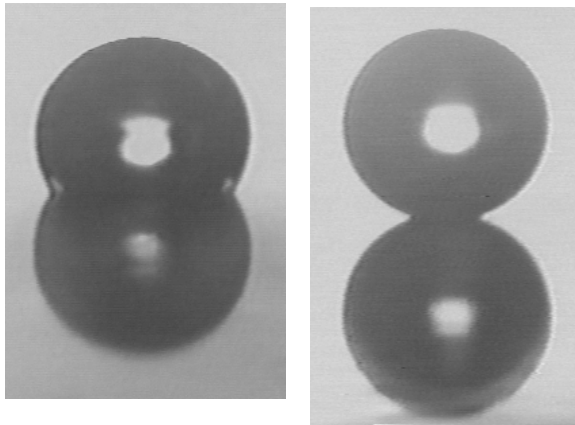
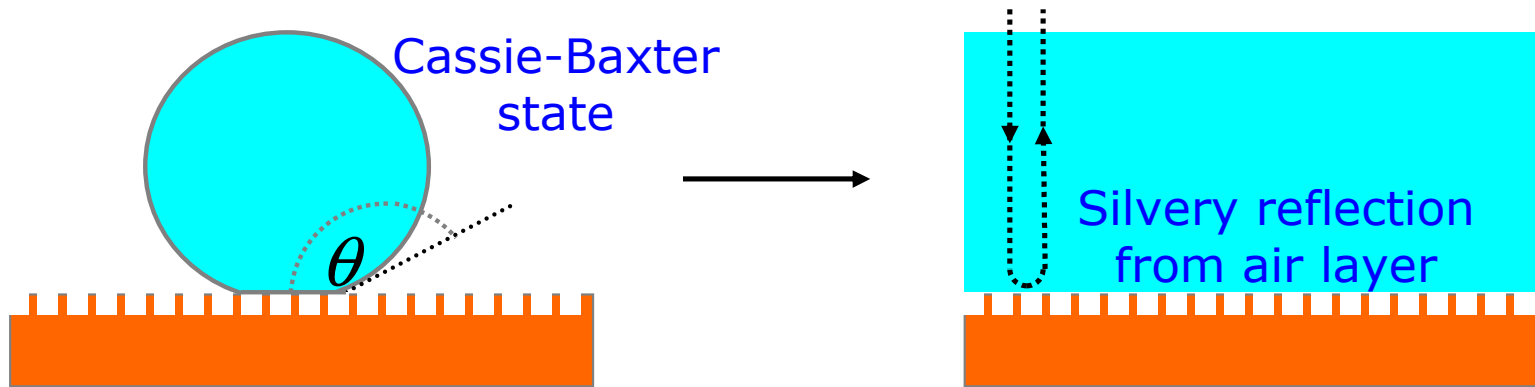


# Current Work: Superhydrophobicity

## Immersed Superhydrophobic Surfaces

Provided design of features correct, penetration of water can be resisted

A silvery sheen can be seen when immersed – due to surface retained layer of air.



## Hydrophobicity and Acoustics

*What might happen when an acoustic wave device has a hydrophobic, or a structured hydrophobic or even a superhydrophobic surface?*

# Usual Hydrodynamic View of Acoustic Response

## Mathematical Formulation

Wave equation for substrate and solid layer or Navier-Stokes equations for liquid  
define substrate and layer/fluid displacements

Match solutions at boundary (substrate-air, substrate-layer or substrate-liquid)

Provides dispersion equation and solution gives resonances

## No-Slip Boundary Condition

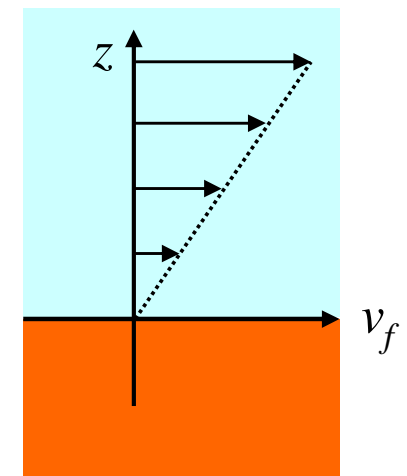
**Solid-Air**  $\Rightarrow q_s(z=0)=q_l(z=0)$  substrate & layer displacements

match at all times

i.e.  $v_s(z=0)=v_l(z=0)$  speeds at wall match

**Solid-Water**  $\Rightarrow v_s(z=0)=v_f(z=0)$  speeds at wall match - fluid

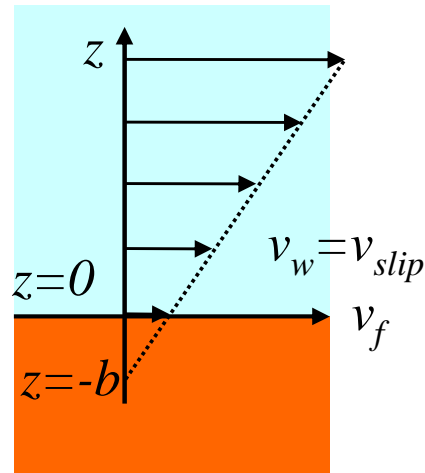
speed extrapolated from bulk



# The Effect of Wall Slip: Theory

## Flow Profile

With slip length,  $b$



Slip length,  $b$ , models effective position of interface  
 Negative  $b$  implies effective interface moves to  
 liquid side of boundary

## Equations

Match speeds

$$v_s(z=0) = v_f(z=-b)$$

Expand

$$v_w - v_f(z=0) = -b \left( \frac{\partial v_f}{\partial z} \right)_{z=0}$$

Force exerted on wall  
 divided by viscosity

*Slip length is a mechanism for modelling an effective average boundary  
 and/or taking into account liquid-solid interfacial forces*

# Effective Sauerbrey “Trapped Liquid Mass”

## Equations of Motion

Solve with slip boundary condition for acoustic impedance  
 Consider in terms of slip length and  
 interpret solution for small  $b$

$$Z_L^{slip} \approx \frac{Z_L^{no\ slip}}{1 + \frac{b}{\eta_f} Z_L^{no\ slip}}$$

## Newtonian Liquid

Kanazawa & Gordon result for no-slip  
 modified by “slip” correction using  $b/\delta$

$$\left(\frac{\Delta\omega}{\omega}\right)_{slip} \approx \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} \left(1 - \frac{2b}{\delta}\right)$$

Slip length to penetration depth ratio

## Negative Slip Length

Define a liquid mass as  $\Delta m_f = b\rho_f$

$$\left(\frac{\Delta\omega}{\omega}\right)_{additional} \approx \left(-\frac{2b}{\delta}\right) \left(\frac{\Delta\omega}{\omega}\right)_{no\ slip} = \frac{\omega\Delta m_f}{\pi\sqrt{\mu_s\rho_s}}$$

*Kanazawa & Gordon viscosity-density product contribution + trapped “Sauerbrey-like liquid mass”, but this assumes all locations are equal, i.e. complete liquid penetration.*

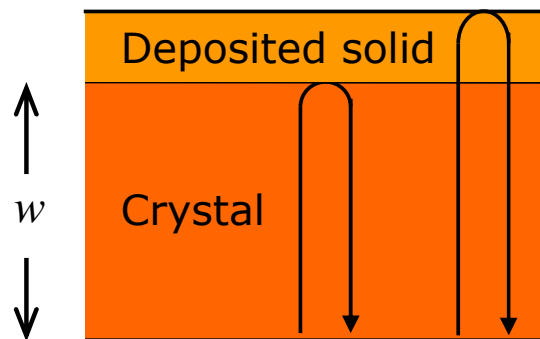


# Implicit Assumptions: Acoustic Reflection View

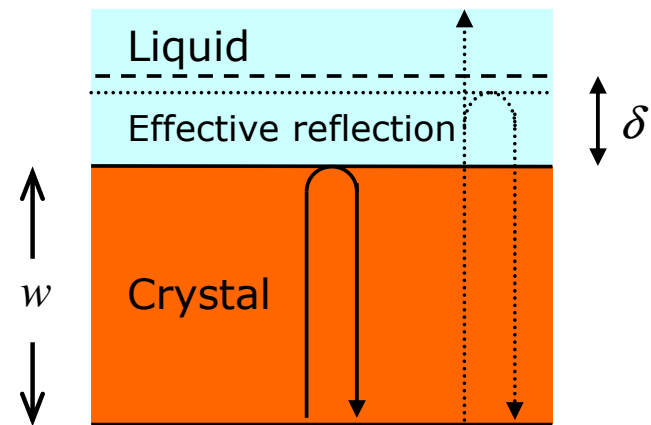
## Simple Cavities and Standing Waves

Solid-Air  $\Rightarrow$  Uniform and strong reflection

Solid-Water  $\Rightarrow$  Partial reflection at an effective plane within penetration depth



Cavity length increases:  $f_{\downarrow}$   
Reflection remains strong



Cavity length increases:  $f_{\downarrow}$   
Reflection becomes partial:  $B_{\uparrow}$

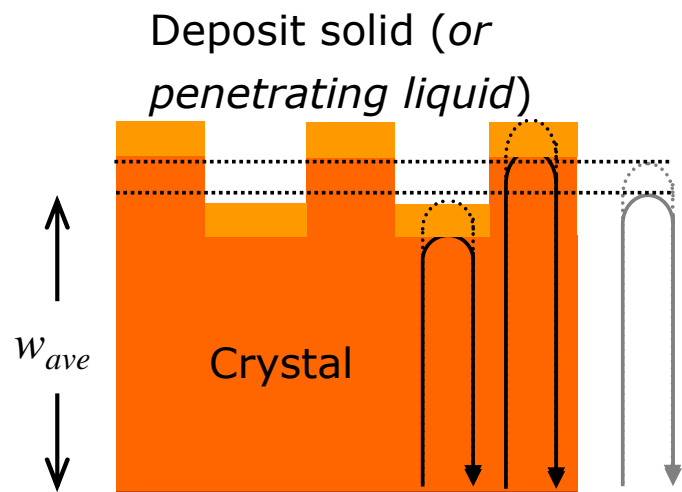
*Assumes reflection from all locations along the surface are of equal strength*

# Effect of Topography and Hydrophobicity?

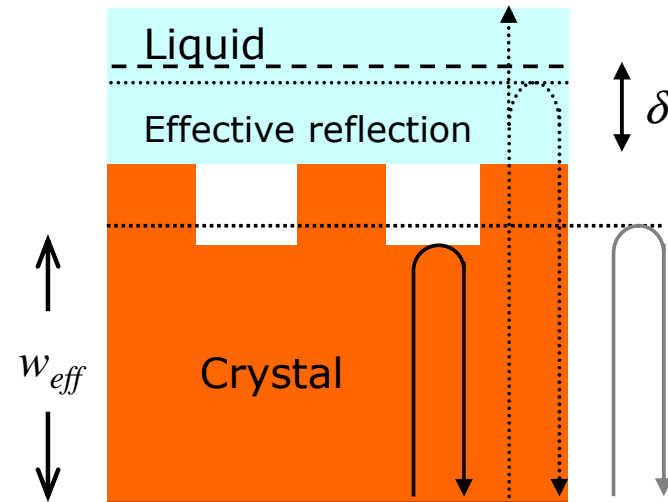
## Structured Cavities and Standing Waves

**Air contact** ⇒ Equally strong reflections from peaks and troughs of surface

**Water contact** ⇒ Changes cavity length and strength of reflection defined by peaks



Effective cavity length  
Peaks and trough increase  
cavity lengths equally:  $f_{\downarrow}$



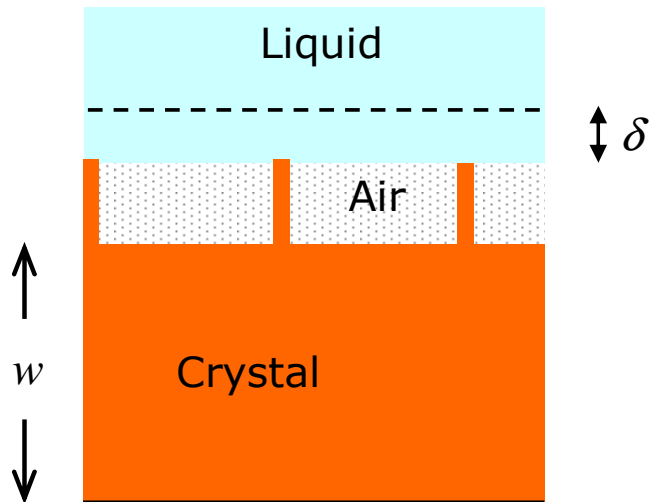
Effective cavity length increased? i.e.  $f_{\downarrow}$   
Or top reflection weakened? If lower  
cavity length becomes dominant:  $f_{\uparrow}$

*Skating form of superhydrophobicity offers possibility of new liquid phase responses*

# Extreme Superhydrophobic Case

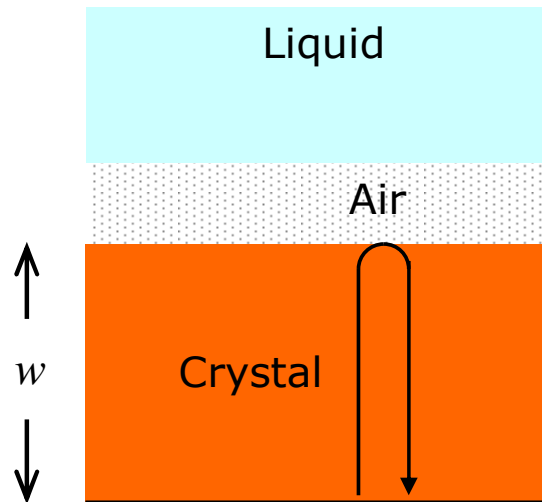
Water immersion  $\Rightarrow$  Water skates across surface features and pressure (or other force) is needed to force capillary penetration

## Superhydrophobic



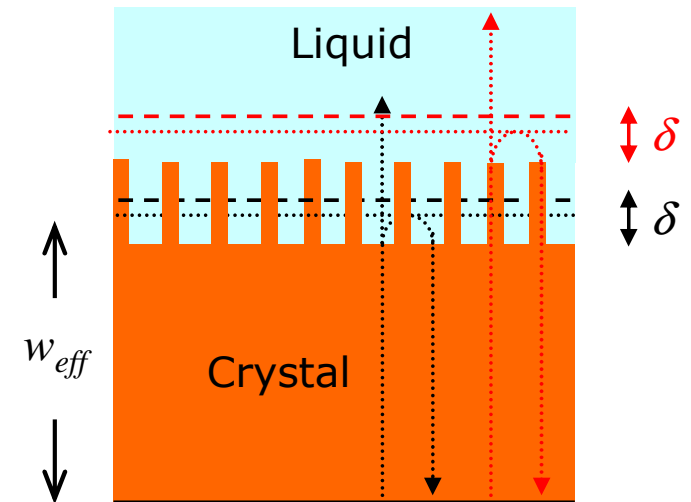
Coupling to liquid is at vanishingly small number of points

## Conceptually



Crystal does not sense the liquid. No significant changes in frequency or bandwidth i.e.  $f_{\downarrow}$  and  $B_{\uparrow} \ll$  K&G values

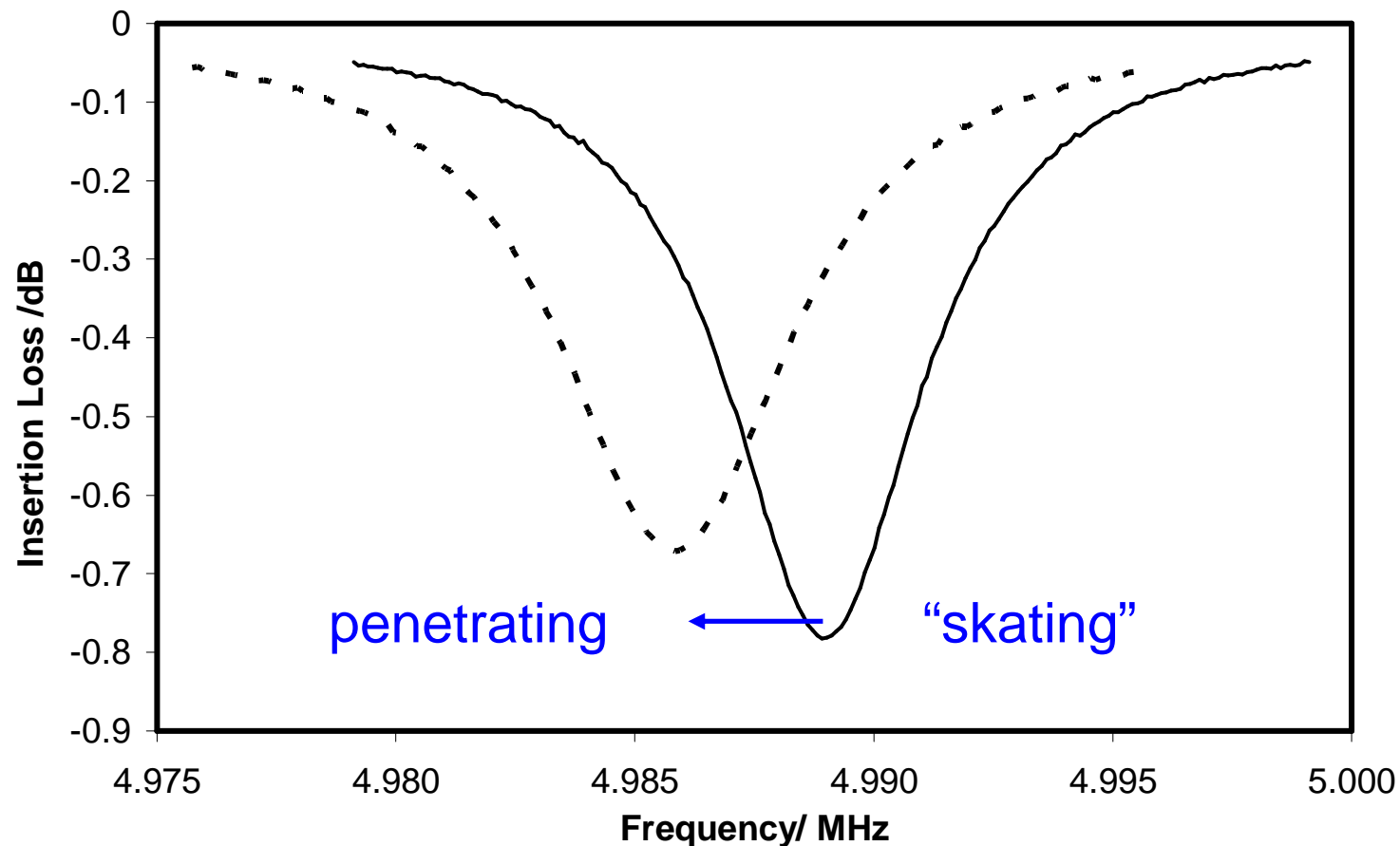
## Wenzel/Penetrating



Coupling across troughs. Effective cavity length increases and reflection weakened, i.e.  $f_{\downarrow}$  and  $B_{\uparrow}$

*QCM behaves as if decoupled from the liquid, unless liquid penetrates into structure*

# QCM with Microposts: “Skating” Transition

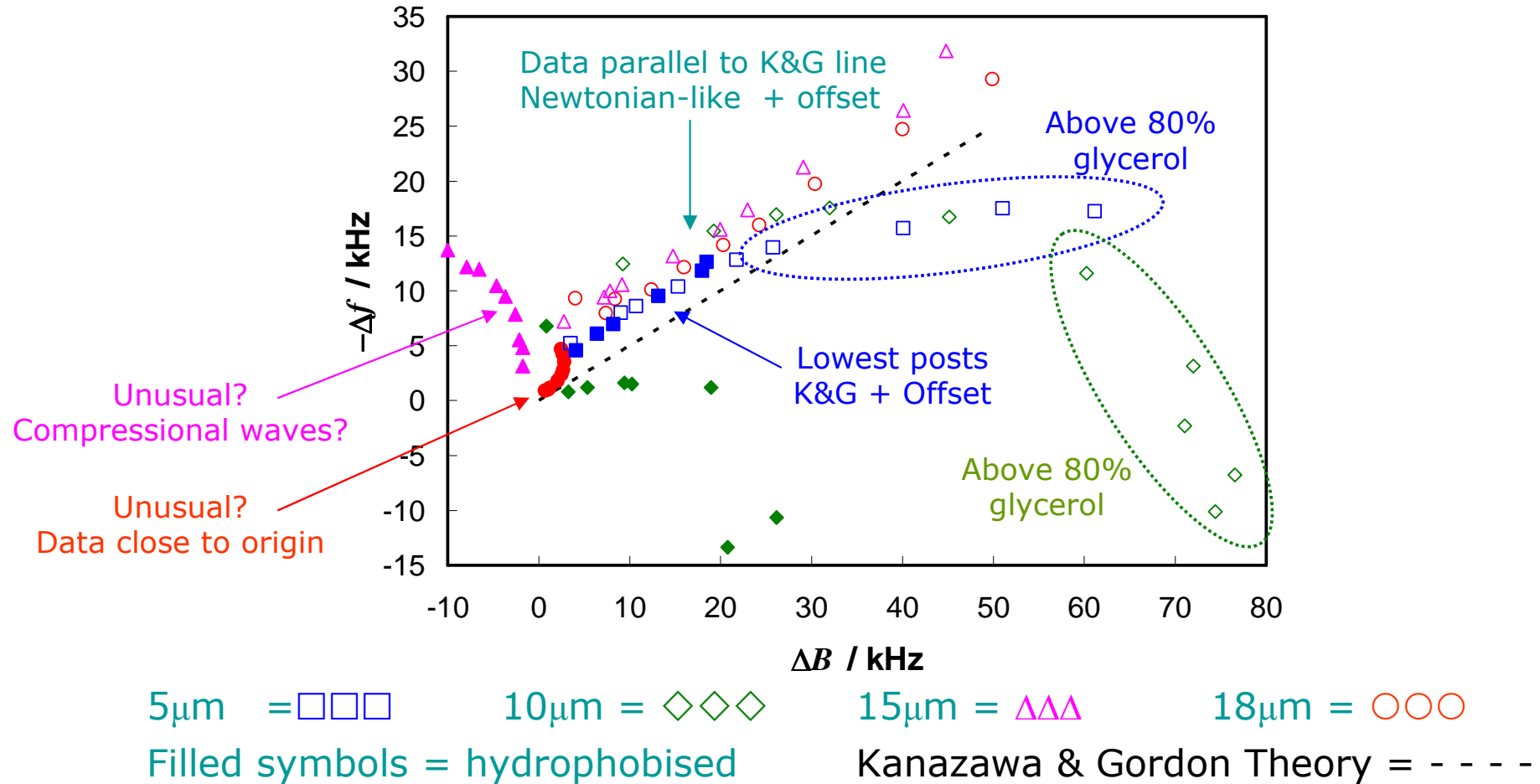


Hydrophobised 18  $\mu\text{m}$  micro-posts. Solid-line is Before pressure applied. Dotted curves is after pressure is applied.

Visually confirmed water ingress after pressure applied

# Micro-Post Surfaces – Water/Glycerol Mixtures

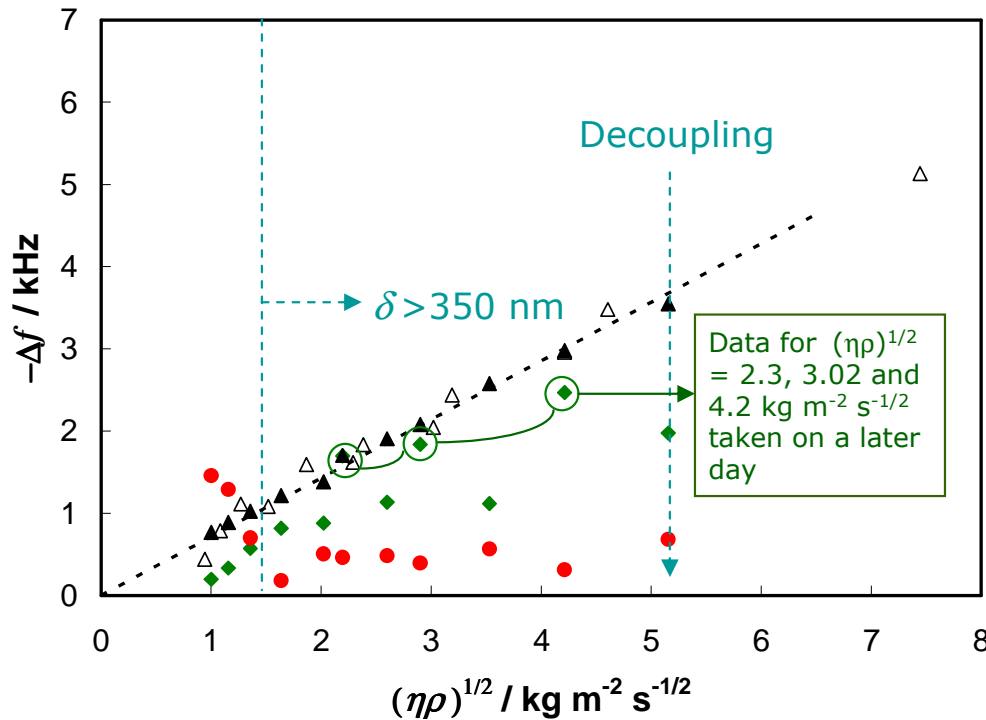
Bare (non-hydrophobised) and Hydrophobised (0-100%)



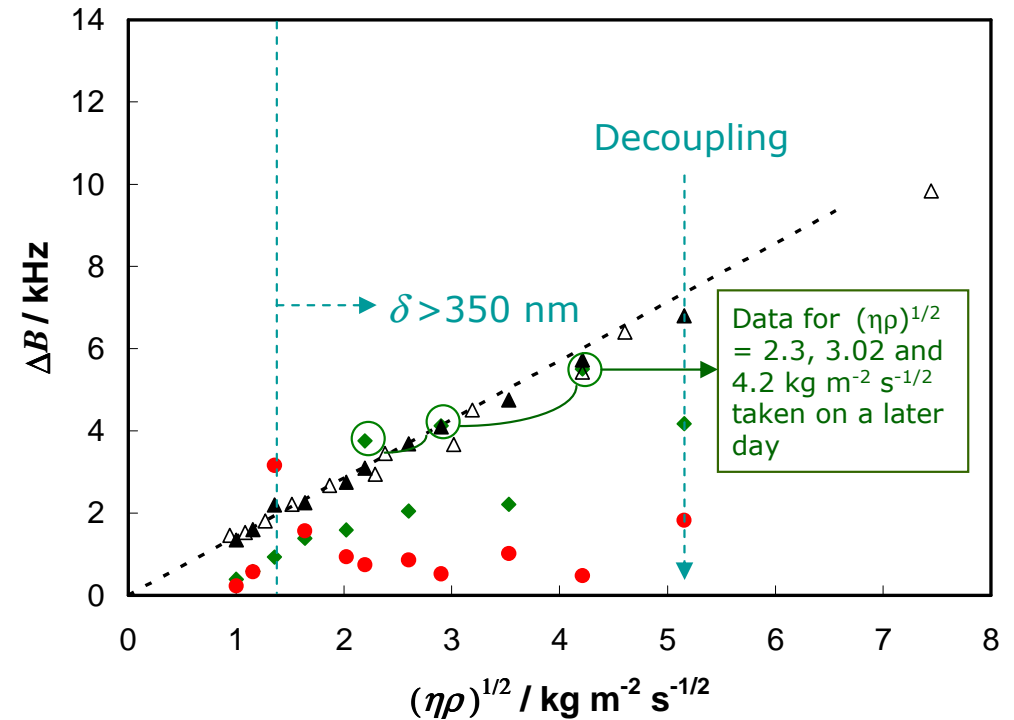
*Hydrophobisation of posts changes type of response – all data generally closer to origin*

# SiO<sub>2</sub> Surfaces: Viscosity-Density

Frequency



Bandwidth



Blank at 25 °C =  $\Delta\Delta\Delta$

Hydrophobic crystal at 20°C =  $\blacktriangle\blacktriangle\blacktriangle$

a1 (Super?)hydrophobic SiO<sub>2</sub> =  $\blacklozenge\blacklozenge\blacklozenge$  at 20 °C

b1 Superhydrophobic SiO<sub>2</sub> =  $\bullet\bullet\bullet$  at 20 °C

*a1: most data points show reduction below K&G levels, later data are at K&G levels*

*b1: data has stronger decoupling trend – consistent with contact angle data/mobile drop*

# Conclusions

## 1. Acoustic Wave Devices

- Many modes for liquid and gas phase operation
- Well established as effective sensors in simple systems

## 2. Current Research on Sensors

- Sperm motility using simple swim time and effective “mass”
- Lab-on-a-Chip for ionic liquids + traps to separate viscosity

## 3. Hydrophobic Surfaces

- Response depends on combination of topography and hydrophobicity
- “Slippy” superhydrophobic surfaces should decouple acoustic response
- Skating-to-penetrating transition could be used as a sensor principle

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The End

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## Collaborators

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